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*Technical Specification*

## Digital cellular telecommunications system (Phase 2+); Modulation (3GPP TS 45.004 version 9.1.0 Release 9)

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# Foreword

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# 1 Scope

The modulator receives the bits from the encryption unit, see 3GPP TS 45.001, and produces an RF signal. The filtering of the Radio Frequency (RF) signal necessary to obtain the spectral purity is not defined, neither are the tolerances associated with the theoretical filter requirements specified. These are contained in 3GPP TS 45.005.

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## 1.1 References

The following documents contain provisions which, through reference in this text, constitute provisions of the present document.

- References are either specific (identified by date of publication, edition number, version number, etc.) or non-specific.
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- For a non-specific reference, the latest version applies. In the case of a reference to a 3GPP document (including a GSM document), a non-specific reference implicitly refers to the latest version of that document *in the same Release as the present document*.

- [1] 3GPP TR 21.905: 'Vocabulary for 3GPP Specifications'.
- [2] 3GPP TS 45.001: 'Physical Layer on the Radio Path (General Description)'.
- [3] 3GPP TS 45.002: 'Multiplexing and multiple access on the radio path'.
- [4] 3GPP TS 45.005: 'Radio transmission and reception'.
- [5] 3GPP TS 45.010: 'Radio subsystem synchronization'.
- [6] 3GPP TS 44.060: 'Radio Link Control/ Medium Access Control (RLC/MAC) protocol'.

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## 1.2 Abbreviations

Abbreviations used in this specification are listed in 3GPP TR 21.905. In addition to abbreviations in 3GPP TR 21.905 the following abbreviation apply:

AQPSK      Adaptive Quadrature Phase Shift Keying

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# 2 Modulation format for GMSK

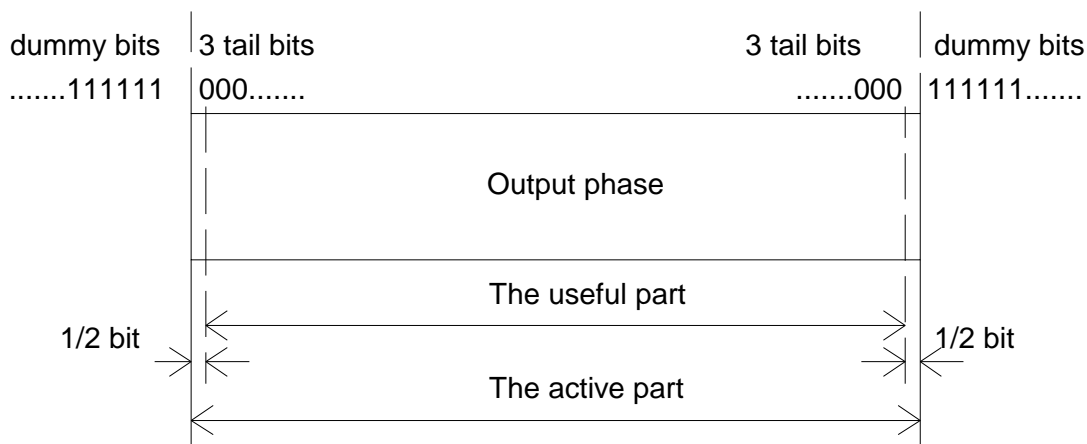
## 2.1 Modulating symbol rate

The modulating symbol rate is the normal symbol rate which is defined as  $1/T = 1\ 625/6$  ksymb/s (i.e. approximately 270.833 ksymb/s), which corresponds to  $1\ 625/6$  kbit/s (i.e. 270.833 kbit/s). T is the normal symbol period (see 3GPP TS 45.010).

## 2.2 Start and stop of the burst

Before the first bit of the bursts as defined in 3GPP TS 45.002 enters the modulator, the modulator has an internal state as if a modulating bit stream consisting of consecutive ones ( $d_i = 1$ ) had entered the differential encoder. Also after the last bit of the time slot, the modulator has an internal state as if a modulating bit stream consisting of consecutive ones

$(d_i = 1)$  had continued to enter the differential encoder. These bits are called dummy bits and define the start and the stop of the active and the useful part of the burst as illustrated in figure 1. Nothing is specified about the actual phase of the modulator output signal outside the useful part of the burst.



**Figure 1: Relation between active part of burst, tail bits and dummy bits. For the normal burst the useful part lasts for 147 modulating bits**

### 2.3 Differential encoding

Each data value  $d_i = [0,1]$  is differentially encoded. The output of the differential encoder is:

$$\hat{d}_i = d_i \oplus d_{i-1} \quad (d_i \in \{0,1\})$$

where  $\oplus$  denotes modulo 2 addition.

The modulating data value  $\alpha_i$  input to the modulator is:

$$\alpha_i = 1 - 2\hat{d}_i \quad (\alpha_i \in \{-1,+1\})$$

### 2.4 Filtering

The modulating data values  $\alpha_i$  as represented by Dirac pulses excite a linear filter with impulse response defined by:

$$g(t) = h(t) * \text{rect}\left(\frac{t}{T}\right)$$

where the function  $\text{rect}(x)$  is defined by:

$$\text{rect}\left(\frac{t}{T}\right) = \frac{1}{T} \quad \text{for } |t| < \frac{T}{2}$$

$$\text{rect}\left(\frac{t}{T}\right) = 0 \quad \text{otherwise}$$

and  $*$  means convolution.  $h(t)$  is defined by:

$$h(t) = \frac{\exp\left(\frac{-t^2}{2\delta^2 T^2}\right)}{\sqrt{(2\pi) \cdot \delta T}}$$

where  $\delta = \frac{\sqrt{\ln(2)}}{2\pi BT}$  and  $BT = 0.3$

where B is the 3 dB bandwidth of the filter with impulse response  $h(t)$ . This theoretical filter is associated with tolerances defined in 3GPP TS 45.005.

## 2.5 Output phase

The phase of the modulated signal is:

$$\varphi(t') = \sum_i \alpha_i \pi h \int_{-\infty}^{t'-iT} g(u) du$$

where the modulating index  $h$  is 1/2 (maximum phase change in radians is  $\pi/2$  per data interval).

The time reference  $t' = 0$  is the start of the active part of the burst as shown in figure 1. This is also the start of the bit period of bit number 0 (the first tail bit) as defined in 3GPP TS 45.002.

## 2.6 Modulation

The modulated RF carrier, except for start and stop of the TDMA burst may therefore be expressed as:

$$x(t') = \sqrt{\frac{2E_c}{T}} \cdot \cos(2\pi f_0 t' + \varphi(t') + \varphi_0)$$

where  $E_c$  is the energy per modulating bit,  $f_0$  is the centre frequency and  $\varphi_0$  is a random phase and is constant during one burst.

# 3 Modulation format for 8PSK

## 3.1 Modulating symbol rate

The modulating symbol rate is the normal symbol rate which is defined as  $1/T = 1\ 625/6$  ksymb/s (i.e. approximately 270.833 ksymb/s), which corresponds to  $3 \cdot 1\ 625/6$  kbit/s (i.e. 812.5 kbit/s). T is the normal symbol period (see 3GPP TS 45.010).

## 3.2 Symbol mapping

The modulating bits are Gray mapped in groups of three to 8PSK symbols by the rule

$$s_l = e^{j2\pi l/8}$$

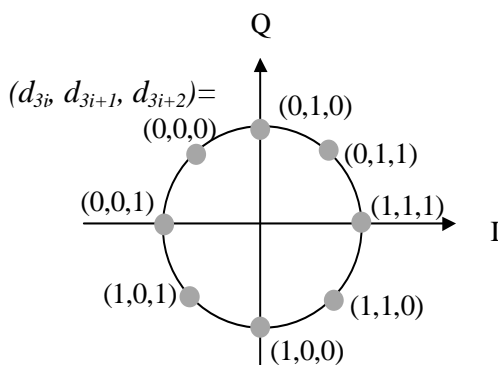
where  $l$  is given by table 1.



**Table 1: Mapping between modulating bits and the 8PSK symbol parameter  $l$ .**

Modulating bits $d_{3i}, d_{3i+1}, d_{3i+2}$	Symbol parameter $l$
(1,1,1)	0
(0,1,1)	1
(0,1,0)	2
(0,0,0)	3
(0,0,1)	4
(1,0,1)	5
(1,0,0)	6
(1,1,0)	7

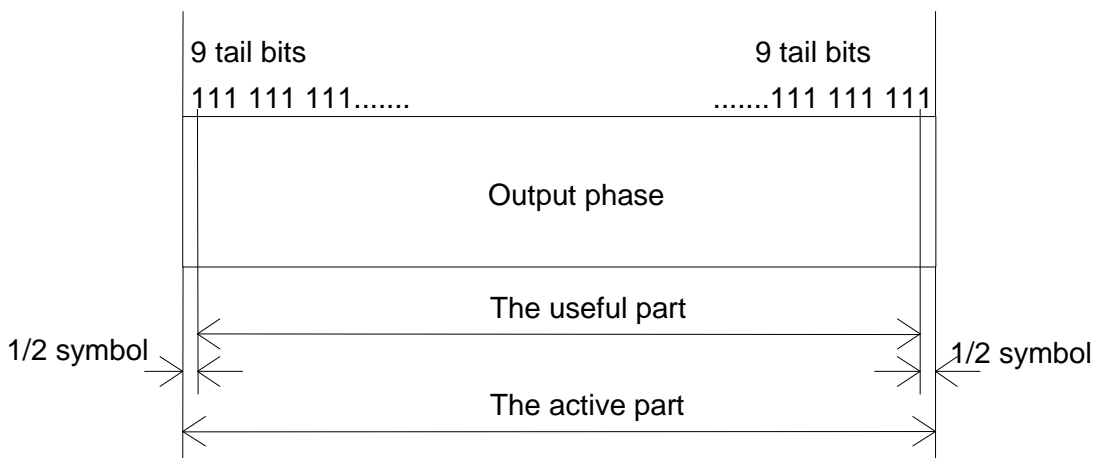
This is illustrated in figure 2.



**Figure 2: Symbol mapping of modulating bits into 8PSK symbols.**

### 3.3 Start and stop of the burst

Before the first bit of the bursts as defined in 3GPP TS 45.002 enters the modulator, the state of the modulator is undefined. Also after the last bit of the burst, the state of the modulator is undefined. The tail bits (see 3GPP TS 45.002) define the start and the stop of the active and the useful part of the burst as illustrated in figure 3. Nothing is specified about the actual phase of the modulator output signal outside the useful part of the burst.



**Figure 3: Relation between active part of burst and tail bits. For the normal burst the useful part lasts for 147 modulating symbols**

### 3.4 Symbol rotation

The 8PSK symbols are continuously rotated with  $3\pi/8$  radians per symbol before pulse shaping. The rotated symbols are defined as

$$\hat{s}_i = s_i \cdot e^{j3\pi/8}$$

### 3.5 Pulse shaping

The modulating 8PSK symbols  $\hat{s}_i$  as represented by Dirac pulses excite a linear pulse shaping filter. This filter is a linearised GMSK pulse, i.e. the main component in a Laurant decomposition of the GMSK modulation. The impulse response is defined by:

$$c_0(t) = \begin{cases} \prod_{i=0}^3 S(t+iT), & \text{for } 0 \leq t \leq 5T \\ 0, & \text{else} \end{cases}$$

where

$$S(t) = \begin{cases} \sin(\pi \int_0^t g(t') dt'), & \text{for } 0 \leq t \leq 4T \\ \sin(\frac{\pi}{2} - \pi \int_0^{t-4T} g(t') dt'), & \text{for } 4T < t \leq 8T \\ 0, & \text{else} \end{cases}$$

$$g(t) = \frac{1}{2T} \left( Q\left(2\pi \cdot 0.3 \frac{t-5T/2}{T\sqrt{\log_e(2)}}\right) - Q\left(2\pi \cdot 0.3 \frac{t-3T/2}{T\sqrt{\log_e(2)}}\right) \right)$$

and

$$Q(t) = \frac{1}{\sqrt{2\pi}} \int_t^{\infty} e^{-\frac{\tau^2}{2}} d\tau.$$

The base band signal is

$$y(t') = \sum_i \hat{s}_i \cdot c_0(t'-iT + 2T)$$

The time reference  $t' = 0$  is the start of the active part of the burst as shown in figure 3. This is also the start of the symbol period of symbol number 0 (containing the first tail bit) as defined in 3GPP TS 45.002.

### 3.6 Modulation

The modulated RF carrier during the useful part of the burst is therefore:

$$x(t') = \sqrt{\frac{2E_s}{T}} \operatorname{Re} \left[ y(t') \cdot e^{j(2\pi f_0 t' + \varphi_0)} \right]$$

where  $E_s$  is the energy per modulating symbol,  $f_0$  is the centre frequency and  $\varphi_0$  is a random phase and is constant during one burst.

## 4 Modulation format for 16QAM and 32QAM at the normal symbol rate

### 4.1 Modulating symbol rate

The modulating symbol rate is the normal symbol rate which is defined as  $1/T = 1625/6$  ksymb/s (i.e. approximately 270.833 ksymb/s), which corresponds to  $4 \cdot 1625/6$  kbit/s (i.e. approximately 1083.3 kbit/s) for 16QAM and to  $5 \cdot 1625/6$  kbit/s (i.e. approximately 1354.2 kbit/s) for 32QAM.  $T$  is the normal symbol period (see 3GPP TS 45.010).

### 4.2 Symbol mapping

The modulating bits are mapped to symbols according to Table 2 for 16QAM and Table 3 for 32QAM.

**Table 2: Mapping between modulating bits and 16QAM symbols.**

Modulating bits $d_{4i}, d_{4i+1}, d_{4i+2}, d_{4i+3}$	16QAM symbol $s_i$	
	I	Q
(0,0,0,0)	$1/\sqrt{10}$	$1/\sqrt{10}$
(0,0,0,1)	$1/\sqrt{10}$	$3/\sqrt{10}$
(0,0,1,0)	$3/\sqrt{10}$	$1/\sqrt{10}$
(0,0,1,1)	$3/\sqrt{10}$	$3/\sqrt{10}$
(0,1,0,0)	$1/\sqrt{10}$	$-1/\sqrt{10}$
(0,1,0,1)	$1/\sqrt{10}$	$-3/\sqrt{10}$
(0,1,1,0)	$3/\sqrt{10}$	$-1/\sqrt{10}$
(0,1,1,1)	$3/\sqrt{10}$	$-3/\sqrt{10}$
(1,0,0,0)	$-1/\sqrt{10}$	$1/\sqrt{10}$
(1,0,0,1)	$-1/\sqrt{10}$	$3/\sqrt{10}$
(1,0,1,0)	$-3/\sqrt{10}$	$1/\sqrt{10}$
(1,0,1,1)	$-3/\sqrt{10}$	$3/\sqrt{10}$
(1,1,0,0)	$-1/\sqrt{10}$	$-1/\sqrt{10}$
(1,1,0,1)	$-1/\sqrt{10}$	$-3/\sqrt{10}$
(1,1,1,0)	$-3/\sqrt{10}$	$-1/\sqrt{10}$
(1,1,1,1)	$-3/\sqrt{10}$	$-3/\sqrt{10}$

Table 3: Mapping between modulating bits and 32QAM symbols.

Modulating bits $d_{5i}, d_{5i+1}, d_{5i+2}, d_{5i+3}, d_{5i+4}$	32QAM symbol $s_i$	
	I	Q
(0,0,0,0,0)	$-3/\sqrt{20}$	$-5/\sqrt{20}$
(0,0,0,0,1)	$-1/\sqrt{20}$	$-5/\sqrt{20}$
(0,0,0,1,0)	$-3/\sqrt{20}$	$5/\sqrt{20}$
(0,0,0,1,1)	$-1/\sqrt{20}$	$5/\sqrt{20}$
(0,0,1,0,0)	$-5/\sqrt{20}$	$-3/\sqrt{20}$
(0,0,1,0,1)	$-5/\sqrt{20}$	$-1/\sqrt{20}$
(0,0,1,1,0)	$-5/\sqrt{20}$	$3/\sqrt{20}$
(0,0,1,1,1)	$-5/\sqrt{20}$	$1/\sqrt{20}$
(0,1,0,0,0)	$-1/\sqrt{20}$	$-3/\sqrt{20}$
(0,1,0,0,1)	$-1/\sqrt{20}$	$-1/\sqrt{20}$
(0,1,0,1,0)	$-1/\sqrt{20}$	$3/\sqrt{20}$
(0,1,0,1,1)	$-1/\sqrt{20}$	$1/\sqrt{20}$
(0,1,1,0,0)	$-3/\sqrt{20}$	$-3/\sqrt{20}$
(0,1,1,0,1)	$-3/\sqrt{20}$	$-1/\sqrt{20}$
(0,1,1,1,0)	$-3/\sqrt{20}$	$3/\sqrt{20}$
(0,1,1,1,1)	$-3/\sqrt{20}$	$1/\sqrt{20}$
(1,0,0,0,0)	$3/\sqrt{20}$	$-5/\sqrt{20}$
(1,0,0,0,1)	$1/\sqrt{20}$	$-5/\sqrt{20}$
(1,0,0,1,0)	$3/\sqrt{20}$	$5/\sqrt{20}$
(1,0,0,1,1)	$1/\sqrt{20}$	$5/\sqrt{20}$
(1,0,1,0,0)	$5/\sqrt{20}$	$-3/\sqrt{20}$
(1,0,1,0,1)	$5/\sqrt{20}$	$-1/\sqrt{20}$
(1,0,1,1,0)	$5/\sqrt{20}$	$3/\sqrt{20}$
(1,0,1,1,1)	$5/\sqrt{20}$	$1/\sqrt{20}$
(1,1,0,0,0)	$1/\sqrt{20}$	$-3/\sqrt{20}$
(1,1,0,0,1)	$1/\sqrt{20}$	$-1/\sqrt{20}$
(1,1,0,1,0)	$1/\sqrt{20}$	$3/\sqrt{20}$
(1,1,0,1,1)	$1/\sqrt{20}$	$1/\sqrt{20}$
(1,1,1,0,0)	$3/\sqrt{20}$	$-3/\sqrt{20}$
(1,1,1,0,1)	$3/\sqrt{20}$	$-1/\sqrt{20}$
(1,1,1,1,0)	$3/\sqrt{20}$	$3/\sqrt{20}$
(1,1,1,1,1)	$3/\sqrt{20}$	$1/\sqrt{20}$

### 4.3 Start and stop of the burst

Before the first bit of the bursts as defined in 3GPP TS 45.002 enters the modulator, the state of the modulator is undefined. Also after the last bit of the burst, the state of the modulator is undefined. The tail symbols (see 3GPP TS 45.002) define the start and the stop of the active and the useful part of the burst as illustrated in figure 4. Nothing is specified about the actual phase of the modulator output signal outside the useful part of the burst.

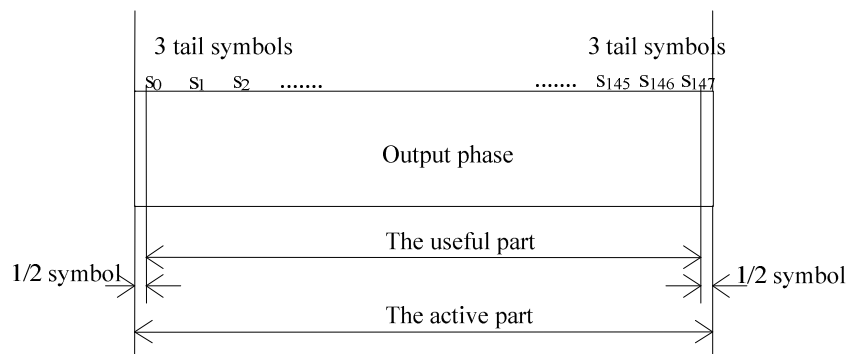


Figure 4: Relation between active part of burst and tail symbols. For the normal burst the useful part lasts for 147 modulating symbols.

## 4.4 Symbol rotation

The symbols are continuously rotated with  $\phi$  radians per symbol before pulse shaping, where  $\phi = \pi/4$  and  $-\pi/4$  for 16QAM and 32QAM respectively. The rotated symbols are defined as

$$\hat{s}_i = s_i \cdot e^{j i \phi}$$

## 4.5 Pulse shaping

The modulating symbols  $\hat{s}_i$  as represented by Dirac pulses excite a linear pulse shaping filter. This filter is the linearised GMSK pulse as defined in 3.5.

## 4.6 Modulation

The modulated RF carrier during the useful part of the burst is:

$$x(t') = \sqrt{\frac{2E_s}{T}} \operatorname{Re}[y(t') \cdot e^{j(2\pi f_0 t' + \phi_0)}]$$

where  $y(t')$  is the base band signal (see 3.5),  $E_s$  is the energy per modulating symbol,  $f_0$  is the centre frequency and  $\phi_0$  is a random phase and is constant during one burst.

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# 5 Modulation format for QPSK, 16QAM and 32QAM at the higher symbol rate

## 5.1 Modulating symbol rate

The modulating symbol rate is the higher symbol rate which is defined as  $1/T = 325$  ksymb/s, which corresponds to 650 kbit/s for QPSK, to 1300 kbit/s for 16QAM and to 1625 kbit/s for 32QAM.  $T$  is the reduced symbol period (see 3GPP TS 45.010).

## 5.2 Symbol mapping

The modulating bits are mapped to symbols according to Table 4 for QPSK, Table 2 for 16QAM and Table 3 for 32QAM..

**Table 4: Mapping between modulating bits and QPSK symbols.**

Modulating bits $d_{2i}, d_{2i+1}$	QPSK symbol $s_i$	
	I	Q
(0,0)	$1/\sqrt{2}$	$1/\sqrt{2}$
(0,1)	$1/\sqrt{2}$	$-1/\sqrt{2}$
(1,0)	$-1/\sqrt{2}$	$1/\sqrt{2}$
(1,1)	$-1/\sqrt{2}$	$-1/\sqrt{2}$

## 5.3 Start and stop of the burst

Before the first bit of the bursts as defined in 3GPP TS 45.002 enters the modulator, the state of the modulator is undefined. Also after the last bit of the burst, the state of the modulator is undefined. The tail symbols (see 3GPP TS 45.002) define the start and the stop of the active and the useful part of the burst as illustrated in figure 5. Nothing is specified about the actual phase of the modulator output signal outside the useful part of the burst.

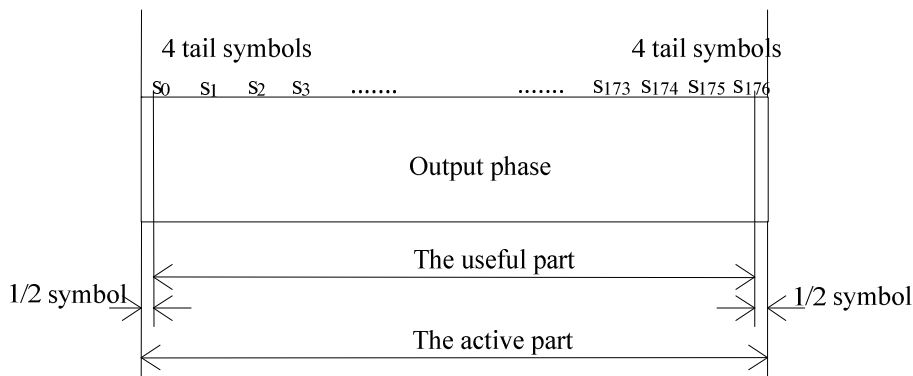


Figure 5: Relation between active part of burst and tail symbols. For the higher symbol rate burst (see 3GPP TS 45.001) the useful part lasts for 176 modulating symbols.

## 5.4 Symbol rotation

The symbols are continuously rotated with  $\phi$  radians per symbol before pulse shaping, where  $\phi = 3\pi/4, \pi/4$  and  $-\pi/4$  for QPSK, 16QAM and 32QAM respectively. The rotated symbols are defined as

$$\hat{s}_i = s_i \cdot e^{ji\phi}$$

## 5.5 Pulse shaping

The modulating symbols  $\hat{s}_i$  as represented by Dirac pulses excite one of the following linear pulse shaping filters:

- A spectrally wide pulse shape  $c'(t)$ , where  $c'(t)$  is the continuous time representation of a discrete time pulse shape  $c_n = c'((n-1)T_s)$ , which is defined in Annex A, where  $T_s$  is the sampling period which for the purpose of the pulse shape definition, is  $T/16$ , and  $n = 1, 2, \dots, 97$ .

The base band signal is

$$y(t') = \sum_i \hat{s}_i \cdot c'(t' - iT + 2.5T)$$

NOTE: A closed-form expression of  $c'(t)$  is not available because the spectrally wide pulse shape was numerically optimised based on a set of discrete filter coefficients. The continuous time function can be obtained by:

- low-pass filtering the discrete time function with a pass-band of 400 kHz and a stop-band beginning at 2600 kHz and;
- truncating the duration to the time interval  $[0, 6T]$ .

An example for such a low-pass filter is a raised cosine filter with the impulse response

$$r(t) = \text{si}(2\pi t \cdot 2600 \text{ kHz}) \cdot \cos(2\pi t \cdot 2200 \text{ kHz}) / (1 - (4 t \cdot 2200 \text{ kHz})^2)$$

with  $\text{si}(x) = \sin(x)/x$ ,

$$\text{resulting in } c'(t) = \sum_{n=1}^{97} c_n r(t - (n-1)T_s) \text{ for } 0 \leq t \leq 6T \text{ and } c'(t) = 0 \text{ for } t < 0 \text{ or } t > 6T.$$

- A spectrally narrow pulse shape,  $c_0(t)$ , which is the linearised GMSK pulse as defined in subclause 3.5 for the normal symbol period.

NOTE: The linearised GMSK pulse is not scaled to the reduced symbol period. Hence its duration in terms of the reduced symbol period is  $6T$ .

The base band signal is

$$y(t') = \sum_i \hat{s}_i \cdot c_0(t' - iT + 2.5T)$$

The time reference  $t' = 0$  is the start of the active part of the burst as shown in figure 3. This is also the start of the symbol period of symbol number 0 (containing the first tail bit) as defined in 3GPP TS 45.002.

For the uplink, the pulse shape that shall be used when transmitting a burst is dependent on the parameter 'Pulse format' that is sent during assignment (see 3GPP TS 44.060). For the downlink the spectrally narrow pulse shape shall be used.

## 5.6 Modulation

The modulated RF carrier during the useful part of the burst is:

$$x(t') = \sqrt{\frac{2E_s}{T}} \text{Re} \left[ y(t') \cdot e^{j(2\pi f_0 t' + \varphi_0)} \right]$$

where  $E_s$  is the energy per modulating symbol,  $f_0$  is the centre frequency and  $\varphi_0$  is a random phase and is constant during one burst.

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## 6 Modulation format for AQPSK

### 6.1 Modulating symbol rate

The modulating symbol rate is the normal symbol rate which is defined as  $1/T = 1 \cdot 625/6$  ksymb/s (i.e. approximately 270,833 ksymb/s), which corresponds to  $2 \cdot 1 \cdot 625/6$  kbit/s (i.e. 541,666 kbit/s).  $T$  is the normal symbol period (see 3GPP TS 45.010).

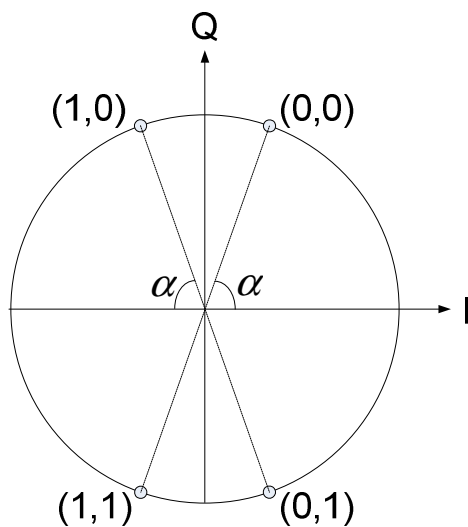
### 6.2 Symbol mapping

The modulating bits are mapped to the quaternary symbols according to Table 5.

**Table 5: Mapping between modulating bits and quaternary symbols.**

Modulating bits for $a_i, b_i$	AQPSK symbol in polar notation $S_i$
(0,0)	$e^{j\alpha}$
(0,1)	$e^{-j\alpha}$
(1,0)	$-e^{-j\alpha}$
(1,1)	$-e^{j\alpha}$

This is illustrated in Figure 5.



**Figure 5: Mapping of modulating bits to AQPSK symbols**

The ratio of power between the Q and I channels is defined as the Subchannel Power Imbalance Ratio (SCPIR).

The value of the SCPIR is given by

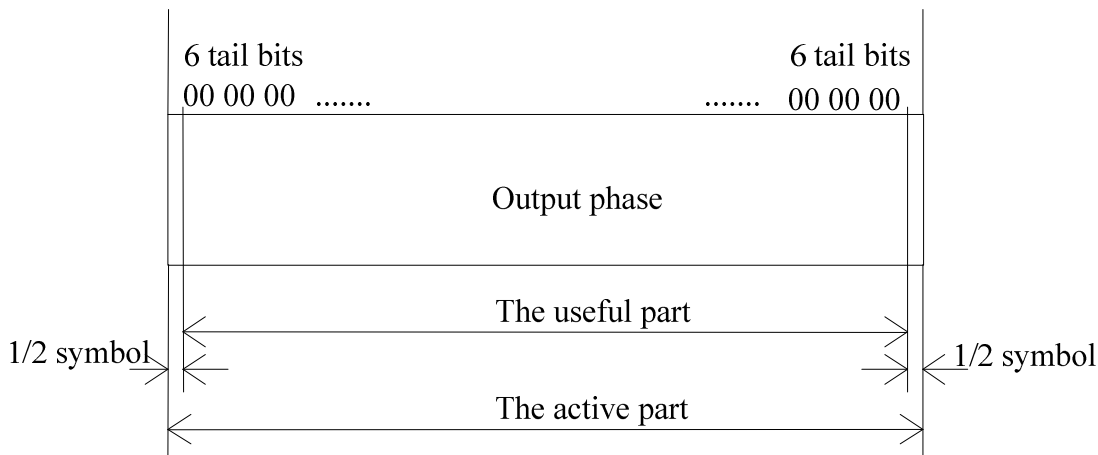
$$SCPIR = 20 \times \log_{10}(\tan(\alpha)) \text{ dB} .$$

The value of  $\alpha$  shall be chosen such that  $|SCPIR| \leq 10 \text{ dB} .$

### 6.3 Start and stop of the burst

Before the first bit of the burst as defined in 3GPP TS 45.002 enters the modulator, the state of the modulator is undefined. Also after the last bit of the burst, the state of the modulator is undefined. The tail symbols (see 3GPP TS 45.002) define the start and the stop of the active and the useful part of the burst as illustrated in Figure 6. Nothing is specified about the actual phase of the modulator output signal outside the useful part of the burst.





**Figure 6: Relation between active part of burst and tail symbols. For the normal burst (see 3GPP TS 45.001) the useful part lasts for 147 modulating symbols.**

### 6.4 Symbol rotation

The symbols are continuously rotated with  $\phi$  radians per symbol before pulse shaping, where  $\phi = \pi/2$ . The rotated symbols are defined as

$$\hat{s}_i = s_i \cdot e^{ji\phi}$$

### 6.5 Pulse shaping

The modulating symbols  $\hat{s}_i$  as represented by Dirac pulses excite the following linear pulse shaping filter:

- $c_0(t)$ , which is the linearised GMSK pulse as defined in subclause 3.5 for the normal symbol period.

The base band signal is

$$y(t') = \sum_i \hat{s}_i \cdot c_0(t' - iT + 2T)$$

The time reference  $t' = 0$  is the start of the active part of the burst as shown in figure 6. This is also the start of the symbol period of symbol number 0 (containing the first tail bit) as defined in 3GPP TS 45.002.

### 6.6 Modulation

The modulated RF carrier during the useful part of the burst is:

$$x(t') = \sqrt{\frac{2E_s}{T}} \operatorname{Re} [ y(t') \cdot e^{j(2\pi f_0 t' + \phi_0)} ]$$

where  $E_s$  is the energy per modulating symbol,  $f_0$  is the centre frequency and  $\phi_0$  is a random phase and is constant during one burst.

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## Annex A (normative): Tx filter coefficients for the spectrally wide pulse shape

For an oversampling factor of 16, i.e. 5200 ksamples/s, there are 97 Tx filter coefficients  $c_1$  to  $c_{97}$  for the spectrally wide pulse shape. The coefficients are symmetric to  $c_{49}$ , i.e.  $c_{49-k} = c_{49+k}$ . The coefficients of  $c_1$  to  $c_{49}$  are listed:

0.00225918460000  
0.00419757900000  
0.00648420700000  
0.00931957020000  
0.01259397500000  
0.01605878900000  
0.01959156100000  
0.02292214900000  
0.02570190500000  
0.02767928100000  
0.02852115300000  
0.02791904300000  
0.02568913000000  
0.02166792700000  
0.01579963100000  
0.00821077000000  
-0.00089211394000  
-0.01114601700000  
-0.02201830600000  
-0.03289439200000  
-0.04302811700000  
-0.05156392200000  
-0.05764086800000  
-0.06034025400000  
-0.05876224400000  
-0.05209962100000  
-0.03961692000000  
-0.02072323500000  
0.00496039200000  
0.03765364500000  
0.07732192300000  
0.12369249000000  
0.17639444000000  
0.23478700000000  
0.29768326000000  
0.36418213000000  
0.43311409000000  
0.50316152000000  
0.57298225000000  
0.64120681000000  
0.70645485000000  
0.76744762000000  
0.82295721000000  
0.87187027000000  
0.91325439000000  
0.94628290000000  
0.97030623000000  
0.98493838000000  
0.99006899000000

## Annex B (informative): Change history

SMG	SPEC	VERS	NEW_VE	PHA	SUBJECT
S27	05.04	5.0.1	6.0.0	R97	Conversion to Release 97 EN
S28	05.04	6.0.0	8.0.0	R99	Introduction of 8PSK for EDGE
S30b	05.04	8.0.0	8.1.0	R99	Correction of mistake for range alpha-sub-i in Clause 2.3
		8.1.0	8.1.1		Figure 3 replaced (as it was corrupted)
G03	05.04	8.1.1	8.2.0	R99	Correction of symbol period notation
G04	45.004	8.2.0	4.0.0	Rel-4	New version for Release 4
G05	45.004	4.0.0	4.1.0	Rel-4	Correction of Timing Alignment for GMSK and 8-PSK Signals

Change history							
Date	TSG #	TSG Doc.	CR	Rev	Subject/Comment	Old	New
2001-11	07	GP-012359	002		Correction of tail bits for 8PSK normal burst	4.1.0	4.2.0
2001-11	07	GP-012372	004		Correction of references to relevant 3GPP TSs	4.1.0	4.2.0
2001-11	07	GP-012360	003		Correction of tail bits for 8PSK normal burst	4.2.0	5.0.0
2002-06	10	GP-021436	005		Corrections and clean up	5.0.0	5.1.0
2003-09					Correction of wrong Release number in the front page	5.1.0	5.1.1
2005-01	23				Version for Release 6	5.1.1	6.0.0
2007-08	35	GP-071544	0006	2	Introduction of QPSK, 16QAM and 32QAM for RED HOT and HUGE	6.0.0	7.0.0
2007-11	36	GP-072015	0008		Spectrally wide pulse shape for HUGE B	7.0.0	7.1.0
2008-02	37	GP-080105	0009		Spectrally wide pulse shape for HUGE B	7.1.0	7.2.0
2008-08	39	GP-081068	0010		Correction of modulating bit rate for 32QAM at the higher symbol rate	7.2.0	7.3.0
2008-12	40				Version for Release 8	7.3.0	8.0.0
2009-12	44				Version for Release 9	8.0.0	9.0.0
2010-05	46	GP-101048	0017	1	Introduction of VAMOS modulation	9.0.0	9.1.0

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# History

<b>Document history</b>		
V9.0.0	February 2010	Publication
V9.1.0	July 2010	Publication