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**Digital cellular telecommunications system (Phase 2+) (GSM);
Specification of the GSM-MILENAGE algorithms: An example
algorithm set for the GSM Authentication and Key Generation
Functions A3 and A8
(3GPP TS 55.205 version 16.0.0 Release 16)**



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Foreword

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Introduction

This document has been prepared by the 3GPP Task Force, and contains an example set of algorithms which may be used as the GSM authentication and key generation functions A3 and A8. (It is not mandatory that the particular algorithms specified in this document are used - the A3 and A8 functions are operator-specifiable rather than being fully standardised).

1 Scope

The present document contains an example set of algorithms which may be used as the GSM authentication and key generation functions A3 and A8. (It is not mandatory that the particular algorithms specified in this document are used - the A3 and A8 functions are operator-specifiable rather than being fully standardised).

Section 3 (normative) introduces the algorithms and describes their input and output parameters. Section 4 (normative) defines the algorithms. Section 5 (informative) describes an alternative algorithm that some operators may prefer. Section 6 (informative) provides test data.

2 References

The following documents contain provisions which, through reference in this text, constitute provisions of the present document.

- References are either specific (identified by date of publication, edition number, version number, etc.) or non-specific.
- For a specific reference, subsequent revisions do not apply.
- For a non-specific reference, the latest version applies. In the case of a reference to a 3GPP document (including a GSM document), a non-specific reference implicitly refers to the latest version of that document *in the same Release as the present document*.

- [1] 3GPP TS 35.206: "3rd Generation Partnership Project; Technical Specification Group Services and System Aspects; 3G Security; Specification of the MILENAGE Algorithm Set: An example algorithm set for the 3GPP authentication and key generation functions f1, f1*, f2, f3, f4, f5 and f5*; Document 2: Algorithm specification".
- [2] 3GPP TS 35.207: "3rd Generation Partnership Project; Technical Specification Group Services and System Aspects; 3G Security; Specification of the MILENAGE Algorithm Set: An example algorithm set for the 3GPP authentication and key generation functions f1, f1*, f2, f3, f4, f5 and f5*; Document 3: Implementors' test data".
- [3] 3GPP TS 35.208: "3rd Generation Partnership Project; Technical Specification Group Services and System Aspects; 3G Security; Specification of the MILENAGE Algorithm Set: An example algorithm set for the 3GPP authentication and key generation functions f1, f1*, f2, f3, f4, f5 and f5*; Document 4: Design conformance test data".
- [4] 3GPP TS 33.102 version 3.10.0: "3rd Generation Partnership Project; Technical Specification Group Services and System Aspects; 3G Security; Security architecture (Release 1999)".
- [5] 3GPP TS 03.20 version 8.1.0: "3rd Generation Partnership Project; Digital cellular telecommunications system (Phase 2+); Security related network functions (Release 1999)".

3 Introductory information (normative)

3.1 Introduction

Within the security architecture of the GSM system there are security functions A3 and A8. The operation of these functions falls completely within the domain of an individual operator, and the functions are therefore to be specified by each operator rather than being fully standardised. The algorithms specified in this document are examples that may be used by an operator who does not wish to design his own.

The inputs and outputs of the two functions are defined in section 3.2.

3.2 Algorithm Inputs and Outputs

The inputs to the algorithms are given in table 1, the outputs in tables 2 and 3 below.

Table 1: Inputs to A3 and A8

| Parameter | Size (bits) | Comment |
|-----------|-------------|--|
| K_i | 128 | Subscriber key $K_i[0] \dots K_i[127]$ |
| RAND | 128 | Random challenge $RAND[0] \dots RAND[127]$ |

Table 2: A3 output

| Parameter | Size (bits) | Comment |
|-----------|-------------|--|
| SRES | 32 | Signed response $SRES[0] \dots SRES[31]$ |

Table 3: A8 output

| Parameter | Size (bits) | Comment |
|-----------|-------------|-----------------------------------|
| K_c | 64 | Cipher key $K_c[0] \dots K_c[63]$ |

3.3 Notation

3.3.1 Bit/Byte ordering

All data variables in this specification are presented with the most significant bit (or byte) on the left hand side and the least significant bit (or byte) on the right hand side. Where a variable is broken down into a number of substrings, the leftmost (most significant) substring is numbered 0, the next most significant is numbered 1, and so on through to the least significant. When a variable, with bit length L , is shown in hexadecimal format, bit 0 is the most significant bit of the leftmost hexadecimal digit, and bit $L-1$ is the least significant bit of the rightmost hexadecimal digit.

3.3.2 List of Symbols

| | |
|----------|--|
| = | The assignment operator. |
| | The concatenation of the two operands. |
| \oplus | The bitwise exclusive-OR operation. |
| $X[i]$ | The i^{th} bit of the variable X . ($X = X[0] X[1] X[2] \dots$). |

4 The GSM-MILENAGE algorithms (normative)

An example algorithm set for UMTS, called MILENAGE (note 1), is specified in [1]. GSM-MILENAGE makes use of MILENAGE.

Specifically, the functions from the UMTS MILENAGE which we make use of are the following (we prefix all input and output names by "MIL3G-" to distinguish them clearly from the inputs and outputs of A3 and A8):

| Function | Inputs | Output |
|-----------|---------------------------------|--|
| f2 | MIL3G-K[0]...MIL3G-K[127] | MIL3G-RES[0]...MIL3G-RES[63] |
| f3 | | MIL3G-CK[0]...MIL3G-CK[127] |
| f4 | | MIL3G-CK[0]...MIL3G-CK[127] |
| | MIL3G-RAND[0]...MIL3G-RAND[127] | MIL3G-CK[64]...MIL3G-CK[127] |
| | | MIL3G-CK[0]...MIL3G-CK[63] ⊕ MIL3G-CK[64]...MIL3G-CK[127] ⊕ MIL3G-CK[0]...MIL3G-CK[63] ⊕ MIL3G-CK[64]...MIL3G-CK[127] |

The GSM-MILENAGE functions are defined as follows:

- Let (MIL3G-K[0]...MIL3G-K[127]) = (K_i[0]...K_i[127])
- Let (MIL3G-RAND[0]...MIL3G-RAND[127]) = (RAND[0]...RAND[127])
- Compute MIL3G-RES, MIL3G-CK and MIL3G-CK from MIL3G-K and MIL3G-RAND, using the MILENAGE functions **f2**, **f3**, and **f4** respectively
- Set (K_c[0]...K_c[63]) = (MIL3G-CK[0]...MIL3G-CK[63]) ⊕
(MIL3G-CK[64]...MIL3G-CK[127]) ⊕
(MIL3G-CK[0]...MIL3G-CK[63]) ⊕
(MIL3G-CK[64]...MIL3G-CK[127])
- Derive SRES from MIL3G-RES using an operator-selected **SRES Derivation Function**. This function must be precisely specified for the GSM-MILENAGE A3 algorithm to be fully defined. The two main recommended options are as follows (note 2):
 - Recommended SRES Derivation Function #1:
(SRES[0]...SRES[31]) = (MIL3G-RES[0]...MIL3G-RES[31]) ⊕ (MIL3G-RES[32]...MIL3G-RES[63]).
 - Recommended SRES Derivation Function #2:
(SRES[0]...SRES[31]) = (MIL3G-RES[0]...MIL3G-RES[31]).

Alternative SRES Derivation Functions may be specified.

NOTE 1: MILENAGE uses a 128-bit operator-specific constant **OP**; a value has to be assigned to this constant for MILENAGE to be fully specified.

NOTE 2: The 3GPP standard conversion function to derive a GSM SRES of 32 bits from a UMTS XRES of up to 128 bits is as follows [4]:

$SRES = XRES^*1 \text{ xor } XRES^*2 \text{ xor } XRES^*3 \text{ xor } XRES^*4$, where $XRES^*$ is 16 octets long and $XRES^* = XRES$ if $XRES$ is 16 octets long and $XRES^* = XRES \parallel 0...0$ if $XRES$ is shorter than 16 octets, $XRES^*i$ are all 4 octets long and $XRES^* = XRES^*1 \parallel XRES^*2 \parallel XRES^*3 \parallel XRES^*4$

Recommended SRES Derivation Function #1 is the result of applying this standard conversion function to a 64-bit XRES equal to MIL3G-RES[0]...MIL3G-RES[63] from MILENAGE. Recommended SRES Derivation Function #2 is the result of applying this standard conversion function to a 32-bit XRES equal to MIL3G-RES[0]...MIL3G-RES[31] from MILENAGE.

5 An alternative algorithm (informative)

The GSM-MILENAGE algorithms defined in section 3 are obtained by applying standard 3G-to-2G conversion functions defined in [4] to the outputs of the UMTS MILENAGE algorithms.

If there is no desire to retain this compatibility with UMTS MILENAGE used in its 2G mode, a much simpler and more efficient algorithm would be to set $TEMP = E_{K_1}(RAND)$, where E is the 128-bit block cipher used as a basic building

block in MILENAGE, i.e. $TEMP$ = the result of encrypting $RAND$ using the key K_i ; then choose non-overlapping substrings of $TEMP$ to be $SRES$ and K_C , e.g. $SRES = TEMP[0]...TEMP[31]$ and $K_C = TEMP[64]...TEMP[127]$.

This alternative does *not* form any part of the GSM-MILENAGE algorithms; it is included just for information.

6 Test data for GSM-MILENAGE (informative)

6.1 Introduction

The test data sets presented here are derived directly from the MILENAGE test sets in [3].

6.2 Format

The format of each test data set is as follows:

| Test Set n | |
|--------------|--|
| K_i | subscriber secret key |
| $RAND$ | random challenge |
| OP | operator-specific MILENAGE constant |
| OP_c | derived from OP and K_i — see [1] |
| MIL3G-RES | MILENAGE f2 output, included for information only |
| SRES#1 | A3 output SRES, if Recommended SRES Derivation Function #1 is used — see section 4, page 7 |
| SRES#2 | A3 output SRES, if Recommended SRES Derivation Function #2 is used — see section 4, page 7 |
| MIL3G-CK | MILENAGE f3 output, included for information only |
| MIL3G-IK | MILENAGE f4 output, included for information only |
| K_c | A8 output (cipher key) |

All test data in this tabular format is shown in hexadecimal representation. The first test set is also shown in binary, to show explicitly the relationship between the binary data and the hexadecimal representation.

6.3 Test Sets

| Test Set 1 in binary format | |
|-----------------------------|---|
| Ki | 01000110 01011011 01011100 11101000 10110001 10011001 10110100 10011111 10101010 01011111 00001010 00101110 11100010 00111000 10100110 10111100 |
| RAND | 00100011 01010101 00111100 10111110 10010110 00110111 10101000 10011101 00100001 10001010 11100110 01001101 10101110 01000111 10111111 00110101 |
| OP | 11001101 11000010 00000010 11010101 00010010 00111110 00100000 11110110 00101011 01101101 01100111 01101010 11000111 00101100 10110011 00011000 |
| OPc | 11001101 01100011 11001011 01110001 10010101 01001010 10011111 01001110 01001000 10100101 10011001 01001110 00110111 10100000 00101011 10101111 |
| MIL3G-RES | 10100101 01000010 00010001 11010101 11100011 10111010 01010000 10111111 |
| SRES#1 | 01000110 11111000 01000001 01101010 |
| SRES#2 | 10100101 01000010 00010001 11010101 |
| MIL3G-CK | 10110100 00001011 10101001 10100011 11000101 10001011 00101010 00000101 10111011 11110000 11011001 10000111 10110010 00011011 11111000 11001011 |
| MIL3G-IK | 11110111 01101001 10111100 11010111 01010001 00000100 01000110 00000100 00010010 01110110 01110010 01110001 00011100 01101101 00110100 01000001 |
| Kc | 11101010 11100100 10111110 10000010 00111010 11111001 10100000 10001011 |

| Test Set 1 | | | | |
|------------|----------|----------|----------|----------|
| Ki | 465b5ce8 | b199b49f | aa5f0a2e | e238a6bc |
| RAND | 23553cbe | 9637a89d | 218ae64d | ae47bf35 |
| OP | cdc202d5 | 123e20f6 | 2b6d676a | c72cb318 |
| OPc | cd63cb71 | 954a9f4e | 48a5994e | 37a02baf |
| MIL3G-RES | a54211d5 | e3ba50bf | | |
| SRES#1 | 46f8416a | | | |
| SRES#2 | a54211d5 | | | |
| MIL3G-CK | b40ba9a3 | c58b2a05 | bbf0d987 | b21bf8cb |
| MIL3G-IK | f769bcd7 | 51044604 | 12767271 | 1c6d3441 |
| Kc | eae4be82 | 3af9a08b | | |

| Test Set 2 | | | | |
|------------|----------|----------|----------|----------|
| Ki | fec86ba6 | eb707ed0 | 8905757b | 1bb44b8f |
| RAND | 9f7c8d02 | 1accf4db | 213ccff0 | c7f71a6a |
| OP | dbc59adc | b6f9a0ef | 735477b7 | fadf8374 |
| OPc | 1006020f | 0a478bf6 | b699f15c | 062e42b3 |
| MIL3G-RES | 8011c48c | 0c214ed2 | | |
| SRES#1 | 8c308a5e | | | |
| SRES#2 | 8011c48c | | | |
| MIL3G-CK | 5dbdbb29 | 54e8f3cd | e665b046 | 179a5098 |
| MIL3G-IK | 59a92d3b | 476a0443 | 487055cf | 88b2307b |
| Kc | aa01739b | 8caa976d | | |

| Test Set 3 | | | | |
|------------|----------|----------|----------|----------|
| Ki | 9e5944ae | a94b8116 | 5c82fbf9 | f32db751 |
| RAND | ce83dbc5 | 4ac0274a | 157c17f8 | 0d017bd6 |
| OP | 223014c5 | 806694c0 | 07ca1eee | f57f004f |
| OPc | a64a507a | e1a2a98b | b88eb421 | 0135dc87 |
| MIL3G-RES | f365cd68 | 3cd92e96 | | |
| SRES#1 | cfbce3fe | | | |
| SRES#2 | f365cd68 | | | |
| MIL3G-CK | e203edb3 | 971574f5 | a94b0d61 | b816345d |
| MIL3G-IK | 0c4524ad | eac041c4 | dd830d20 | 854fc46b |
| Kc | 9a8ec95f | 408cc507 | | |

| Test Set 4 | | | | |
|------------|----------|----------|----------|----------|
| Ki | 4ab1deb0 | 5ca6ceb0 | 51fc98e7 | 7d026a84 |
| RAND | 74b0cd60 | 31a1c833 | 9b2b6ce2 | b8c4a186 |
| OP | 2d16c5cd | 1fdf6b22 | 383584e3 | bef2a8d8 |
| OPc | dcf07cbd | 51855290 | b92a07a9 | 891e523e |
| MIL3G-RES | 5860fc1b | ce351e7e | | |
| SRES#1 | 9655e265 | | | |
| SRES#2 | 5860fc1b | | | |
| MIL3G-CK | 7657766b | 373d1c21 | 38f307e3 | de9242f9 |
| MIL3G-IK | 1c42e960 | d89b8fa9 | 9f2744e0 | 708ccb53 |
| Kc | cdc1dc08 | 41b81a22 | | |

| Test Set 5 | | | | |
|------------|----------|----------|----------|----------|
| Ki | 6c38a116 | ac280c45 | 4f59332e | e35c8c4f |
| RAND | ee6466bc | 96202c5a | 557abbef | f8babf63 |
| OP | 1ba00a1a | 7c6700ac | 8c3ff3e9 | 6ad08725 |
| OPc | 3803ef53 | 63b947c6 | aaa225e5 | 8fae3934 |
| MIL3G-RES | 16c8233f | 05a0ac28 | | |
| SRES#1 | 13688f17 | | | |
| SRES#2 | 16c8233f | | | |
| MIL3G-CK | 3f8c7587 | fe8e4b23 | 3af676ae | de30ba3b |
| MIL3G-IK | a7466cc1 | e6b2a133 | 7d49d3b6 | 6e95d7b4 |
| Kc | df75bc5e | a899879f | | |

| Test Set 6 | | | | |
|------------|----------|----------|----------|----------|
| Ki | 2d609d4d | b0ac5bf0 | d2c0de26 | 7014de0d |
| RAND | 194aa756 | 013896b7 | 4b4a2a3b | 0af4539e |
| OP | 460a4838 | 5427aa39 | 264aac8e | fc9e73e8 |
| OPc | c35a0ab0 | bcdfc925 | 2caff15f | 24efbde0 |
| MIL3G-RES | 8c25a16c | d918a1df | | |
| SRES#1 | 553d00b3 | | | |
| SRES#2 | 8c25a16c | | | |
| MIL3G-CK | 4cd08460 | 20f8fa07 | 31dd47cb | dc6be411 |
| MIL3G-IK | 88ab80a4 | 15f15c73 | 711254a1 | d388f696 |
| Kc | 84b417ae | 3aeab4f3 | | |

| Test Set 7 | | | | |
|------------|----------|----------|----------|----------|
| Ki | a530a7fe | 428fad10 | 82c45edd | fce13884 |
| RAND | 3a4c2b32 | 45c50eb5 | c71d0863 | 9395764d |
| OP | 511c6c4e | 83e38c89 | b1c5d8dd | e62426fa |
| OPc | 27953e49 | bc8af6dc | c6e730eb | 80286be3 |
| MIL3G-RES | a63241e1 | ffc3e5ab | | |
| SRES#1 | 59f1a44a | | | |
| SRES#2 | a63241e1 | | | |
| MIL3G-CK | 10f05bab | 75a99a5f | bb98a9c2 | 87679c3b |
| MIL3G-IK | f9ec0865 | eb32f223 | 69cade40 | c59c3a44 |
| Kc | 3b4e244c | dc60ce03 | | |

| Test Set 8 | | | | |
|------------|----------|----------|----------|----------|
| Ki | d9151cf0 | 4896e258 | 30bf2e08 | 267b8360 |
| RAND | f761e5e9 | 3d603feb | 730e2755 | 6cb8a2ca |
| OP | 75fc2233 | a44294ee | 8e6de25c | 4353d26b |
| OPc | c4c93eff | e8a08138 | c203d4c2 | 7ce4e3d9 |
| MIL3G-RES | 4a90b217 | 1ac83a76 | | |
| SRES#1 | 50588861 | | | |
| SRES#2 | 4a90b217 | | | |
| MIL3G-CK | 71236b71 | 29f9b22a | b77ea7a5 | 4c96da22 |
| MIL3G-IK | 90527eba | a5588968 | db417273 | 25a04d9e |
| Kc | 8d4ec01d | e597acfe | | |

| Test Set 9 | | | | |
|------------|----------|----------|----------|----------|
| Ki | a0e2971b | 6822e8d3 | 54a18cc2 | 35624ecb |
| RAND | 08eff828 | b13fdb56 | 2722c65c | 7f30a9b2 |
| OP | 323792fa | ca21fb4d | 5d6f13c1 | 45a9d2c1 |
| OPc | 82a26f22 | bba9e948 | 8f949a10 | d98e9cc4 |
| MIL3G-RES | 4bc2212d | 8624910a | | |
| SRES#1 | cde6b027 | | | |
| SRES#2 | 4bc2212d | | | |
| MIL3G-CK | 08cef6d0 | 04ec6147 | 1a3c3cda | 048137fa |
| MIL3G-IK | ed0318ca | 5deb9206 | 272f6e8f | a64ba411 |
| Kc | d8debc4f | fbcd60aa | | |

| Test Set 10 | | | | |
|-------------|----------|----------|----------|----------|
| Ki | 0da6f7ba | 86d5eac8 | a19cf563 | ac58642d |
| RAND | 679ac4db | acd7d233 | ff9d6806 | f4149ce3 |
| OP | 4b9a26fa | 459e3acb | ff36f401 | 5de3bdc1 |
| OPc | 0db1071f | 8767562c | a43a0a64 | c41e8d08 |
| MIL3G-RES | 6fc30fee | 6d123523 | | |
| SRES#1 | 02d13acd | | | |
| SRES#2 | 6fc30fee | | | |
| MIL3G-CK | 69b1cae7 | c7429d97 | 5e245cac | b05a517c |
| MIL3G-IK | 74f24e8c | 26df58e1 | b38d7dcd | 4f1b7fbd |
| Kc | f0eaa50a | 1edcebb7 | | |

| Test Set 11 | | | | |
|-------------|----------|----------|----------|----------|
| Ki | 77b45843 | c88e58c1 | 0d202684 | 515ed430 |
| RAND | 4c47eb30 | 76dc55fe | 5106cb20 | 34b8cd78 |
| OP | bf3286c7 | a51409ce | 95724d50 | 3bfe6e70 |
| OPc | d483afae | 562409a3 | 26b5bb0b | 20c4d762 |
| MIL3G-RES | aefa357b | eac2a87a | | |
| SRES#1 | 44389d01 | | | |
| SRES#2 | aefa357b | | | |
| MIL3G-CK | 908c43f0 | 569cb8f7 | 4bc971e7 | 06c36c5f |
| MIL3G-IK | c251df0d | 888dd932 | 9bcf4665 | 5b226e40 |
| Kc | 82dbab7f | 83f063da | | |

| Test Set 12 | | | | |
|-------------|----------|----------|----------|----------|
| Ki | 729b1772 | 9270dd87 | ccdf1bfe | 29b4e9bb |
| RAND | 311c4c92 | 9744d675 | b720f3b7 | e9b1cbd0 |
| OP | d04c9c35 | bd2262fa | 810d2924 | d036fd13 |
| OPc | 228c2f2f | 06ac3268 | a9e616ee | 16db4ba1 |
| MIL3G-RES | 98dbbd09 | 9b3b408d | | |
| SRES#1 | 03e0fd84 | | | |
| SRES#2 | 98dbbd09 | | | |
| MIL3G-CK | 44c0f23c | 5493cfd2 | 41e48f19 | 7e1d1012 |
| MIL3G-IK | 0c9fb816 | 13884c25 | 35dd0eab | f3b440d8 |
| Kc | 3c66cb98 | cab2d33d | | |

| Test Set 13 | | | | |
|-------------|----------|----------|----------|----------|
| Ki | d32dd23e | 89dc6623 | 54ca12eb | 79dd32fa |
| RAND | cf7d0ab1 | d9430695 | 0bf12018 | fb46887 |
| OP | fe75905b | 9da47d35 | 6236d031 | 4e09c32e |
| OPc | d22a4b41 | 80a53257 | 08a5ff70 | d9f67ec7 |
| MIL3G-RES | af4a411e | 1139f2c2 | | |
| SRES#1 | be73b3dc | | | |
| SRES#2 | af4a411e | | | |
| MIL3G-CK | 5af86b80 | edb70df5 | 292cc112 | 1cbad50c |
| MIL3G-IK | 7f4d6ae7 | 440e1878 | 9a8b75ad | 3f42f03a |
| Kc | 9612b5d8 | 8a4130bb | | |

| Test Set 14 | | | | |
|-------------|----------|----------|----------|----------|
| Ki | af7c65e1 | 927221de | 591187a2 | c5987a53 |
| RAND | 1f0f8578 | 464fd59b | 64bed2d0 | 9436b57a |
| OP | 0c7acb8d | 95b7d4a3 | 1c5aca6d | 26345a88 |
| OPc | a4cf5c81 | 55c08a7e | ff418e54 | 43b98e55 |
| MIL3G-RES | 7bffa5c2 | f41fbc05 | | |
| SRES#1 | 8fe019c7 | | | |
| SRES#2 | 7bffa5c2 | | | |
| MIL3G-CK | 3f8c3f3c | cf7625bf | 77fc94bc | fd22fd26 |
| MIL3G-IK | abcbae8f | d46115e9 | 961a55d0 | da5f2078 |
| Kc | 75a150df | 3c6aed08 | | |

| Test Set 15 | | | | |
|-------------|----------|----------|----------|----------|
| Ki | 5bd7ecd3 | d3127a41 | d12539be | d4e7cf71 |
| RAND | 59b75f14 | 251c7503 | 1d0bcbac | 1c2c04c7 |
| OP | f967f760 | 38b920a9 | cd25e10c | 08b49924 |
| OPc | 76089d3c | 0ff3efdc | 6e36721d | 4fceb747 |
| MIL3G-RES | 7e3f44c7 | 591f6f45 | | |
| SRES#1 | 27202b82 | | | |
| SRES#2 | 7e3f44c7 | | | |
| MIL3G-CK | d42b2d61 | 5e49a03a | c275a5ae | f97af892 |
| MIL3G-IK | 0b3f8d02 | 4fe6bfaf | aa982b8f | 82e319c2 |
| Kc | b7f92e42 | 6a36fec5 | | |

| Test Set 16 | | | | |
|-------------|----------|----------|----------|----------|
| Ki | 6cd1c6ce | b1e01e14 | f1b82316 | a90b7f3d |
| RAND | f69b78f3 | 00a0568b | ce9f0cb9 | 3c4be4c9 |
| OP | 078bfca9 | 564659ec | d8851e84 | e6c59b48 |
| OPc | a219dc37 | f1dc7d66 | 738b5843 | c799f206 |
| MIL3G-RES | 70f6bdb9 | ad21525f | | |
| SRES#1 | ddd7efe6 | | | |
| SRES#2 | 70f6bdb9 | | | |
| MIL3G-CK | 6edaf99e | 5bd9f85d | 5f36d91c | 1272fb4b |
| MIL3G-IK | d61c853c | 280dd9c4 | 6f297bae | c386de17 |
| Kc | 88d9de10 | a22004c5 | | |

| Test Set 17 | | | | |
|-------------|----------|----------|----------|----------|
| Ki | b73a90cb | cf3afb62 | 2dba83c5 | 8a8415df |
| RAND | b120f1c1 | a0102a2f | 507dd543 | de68281f |
| OP | b672047e | 003bb952 | dca6cb8a | f0e5b779 |
| OPc | df0c6786 | 8fa25f74 | 8b7044c6 | e7c245b8 |
| MIL3G-RES | 479dd25c | 20792d63 | | |
| SRES#1 | 67e4ff3f | | | |
| SRES#2 | 479dd25c | | | |
| MIL3G-CK | 66195dbe | d0313274 | c5ca7766 | 615fa25e |
| MIL3G-IK | 66bec707 | eb2afc47 | 6d7408a8 | f2927b36 |
| Kc | a819e577 | a8d6175b | | |

| Test Set 18 | | | | |
|-------------|----------|----------|----------|----------|
| Ki | 51222502 | 14c33e72 | 3a5dd523 | fc145fc0 |
| RAND | 81e92b6c | 0ee0e12e | bceba8d9 | 2a99dfa5 |
| OP | c9e87632 | 86b5b9ff | bdf56e12 | 97d0887b |
| OPc | 981d464c | 7c52eb6e | 50362349 | 84ad0bcf |
| MIL3G-RES | 28d7b0f2 | a2ec3de5 | | |
| SRES#1 | 8a3b8d17 | | | |
| SRES#2 | 28d7b0f2 | | | |
| MIL3G-CK | 5349fbe0 | 98649f94 | 8f5d2e97 | 3a81c00f |
| MIL3G-IK | 9744871a | d32bf9bb | d1dd5ce5 | 4e3e2e5a |
| Kc | 9a8d0e88 | 3ff0887a | | |

| Test Set 19 | | | | |
|-------------|----------|----------|----------|----------|
| Ki | 90dca4ed | a45b53cf | 0f12d7c9 | c3bc6a89 |
| RAND | 9fddc720 | 92c6ad03 | 6b6e4647 | 89315b78 |
| OP | 3ffcf5b | 7b111158 | 9920d352 | 8e84e655 |
| OPc | cb9cccc4 | b9258e6d | ca476037 | 9fb82581 |
| MIL3G-RES | a95100e2 | 760952cd | | |
| SRES#1 | df58522f | | | |
| SRES#2 | a95100e2 | | | |
| MIL3G-CK | b5f2da03 | 883b69f9 | 6bf52e02 | 9ed9ac45 |
| MIL3G-IK | b4721368 | bc16ea67 | 875c5598 | 688bb0ef |
| Kc | ed29b2f1 | c27f9f34 | | |

Annex A (informative): Change history

| Change history | | | | | | | | |
|----------------|-------|-----------|------|-----|-----|---|----------|---------------|
| Date | TSG # | TSG Doc. | CR | Rev | Cat | Subject/Comment | Old | New |
| 2002-05 | - | - | - | - | - | ETSI SAGE version 1.0 produced and forwarded to SA WG3 for approval. | | SAGE 1.0 |
| 2002-12 | SP-18 | SP-020724 | - | - | - | Approved by SA WG3 meeting #26 (S3-020675). Editorial update to change MILENAGE-2G to GSM-MILENAGE and correction to references. Updated to 3GPP TS format (Technically equivalent to ETSI SAGE version 1.0). Presentation to TSG SA#18 for approval (Release 6). | SAGE 1.0 | 1.0.0 |
| 2002-12 | SP-18 | - | - | - | - | Approved at TSG SA#18. Updated to Version 6.0.0 for publication (Rel-6) | 1.0.0 | 6.0.0 |
| 2003-12 | SP-22 | SP-030606 | 0001 | - | D | Correction of reference | 6.0.0 | 6.1.0 |
| 2006-03 | SP-31 | SP-060057 | 0002 | - | F | Clarifying the Bit/Byte ordering and symbols for GSM-MILENAGE example algorithm | 6.1.0 | 6.2.0 |
| 2007-06 | SP-36 | - | - | - | - | Update to Rel-7 version (MCC) | 6.2.0 | 7.0.0 |
| 2008-12 | SP-42 | - | - | - | - | Update to Rel-8 version (MCC) | 7.0.0 | 8.0.0 |
| 2009-12 | - | - | - | - | - | Update to Rel-9 version (MCC) | 8.0.0 | 9.0.0 |
| 2011-03 | - | - | - | - | - | Update to Rel-10 version (MCC) | 9.0.0 | 10.0.0 |
| 2012-09 | - | - | - | - | - | Update to Rel-11 version (MCC) | 10.0.0 | 11.0.0 |
| 2014-09 | - | - | - | - | - | Update to Rel-12 version (MCC) | 11.0.0 | 12.0.0 |
| 2016-01 | - | - | - | - | - | Update to Rel-13 version (MCC) | 12.0.0 | 13.0.0 |
| 2017-03 | SA#75 | - | - | - | - | Promotion to Release 14 without technical change | 13.0.0 | 14.0.0 |
| 2018-10 | - | - | - | - | - | Update to Rel-15 version (MCC) | 14.0.0 | 15.0.0 |
| 2020-07 | - | - | - | - | - | Update to Rel-16 version (MCC) | 15.0.0 | 16.0.0 |

History

| Document history | | |
|-------------------------|-------------|-------------|
| V16.0.0 | August 2020 | Publication |
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