

# ETSI TS 155 251 V15.0.0 (2018-07)



**Digital cellular telecommunications system (Phase 2+) (GSM);  
Specification of the GEA5 and GIA5 encryption algorithms for  
General Packet Radio Service (GPRS);  
GEA5 and GIA5 algorithm specification  
(3GPP TS 55.251 version 15.0.0 Release 15)**



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Reference

RTS/TSGS-0355251vf00

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Keywords

GSM,SECURITY

**ETSI**

650 Route des Lucioles  
F-06921 Sophia Antipolis Cedex - FRANCE

Tel.: +33 4 92 94 42 00 Fax: +33 4 93 65 47 16

Siret N° 348 623 562 00017 - NAF 742 C  
Association à but non lucratif enregistrée à la  
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# Foreword

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- y the second digit is incremented for all changes of substance, i.e. technical enhancements, corrections, updates, etc.
- z the third digit is incremented when editorial only changes have been incorporated in the document.

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# Introduction

This specification has been prepared by the 3GPP Task Force, and gives a detailed specification of the 3GPP confidentiality algorithm GEA5 and the 3GPP integrity algorithm GIA5.

This document is the first of three, which between them form the entire specification of the 3GPP confidentiality algorithm GEA5 and the 3GPP integrity algorithm GIA5:

- **3GPP TS 55.251: "Specification of the GEA5 and GIA5 encryption algorithms for GPRS; GEA5 and GIA4 algorithm specification".**
- 3GPP TS 55.252: "Specification of the GEA5 and GIA5 encryption algorithms for GPRS; Implementers' test data".
- 3GPP TS 55.253: "Specification of the GEA5 and GIA5 encryption algorithms for GPRS; Design conformance test data".

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# 1 Scope

The present document defines the technical details of the 3GPP confidential algorithm GEA5 and the 3GPP integrity algorithm GIA5.

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## 2 References

The following documents contain provisions which, through reference in this text, constitute provisions of the present document.

- References are either specific (identified by date of publication, edition number, version number, etc.) or non-specific.
- For a specific reference, subsequent revisions do not apply.
- For a non-specific reference, the latest version applies. In the case of a reference to a 3GPP document (including a GSM document), a non-specific reference implicitly refers to the latest version of that document *in the same Release as the present document*.

[1] 3GPP TR 21.905: "Vocabulary for 3GPP Specifications".

[2] 3GPP TS 33.216: "Specification of the 3GPP Confidentiality and Integrity Algorithms UEA2 & UIA2; Document 2: SNOW 3G specification".

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## 3 Definitions, symbols and abbreviations

### 3.1 Definitions

For the purposes of the present document, the terms and definitions given in 3GPP TR 21.905 [1] and the following apply. A term defined in the present document takes precedence over the definition of the same term, if any, in 3GPP TR 21.905 [1].

(none)

### 3.2 Symbols

For the purposes of the present document, the following symbols apply:

=	The assignment operator.
$\oplus$	The bitwise exclusive-OR operation.
	The concatenation of the two operands.
KASUMI[x] <sub>k</sub>	The output of the KASUMI algorithm applied to input value <b>x</b> using the key <b>k</b> .
X[i]	The <i>i</i> <sup>th</sup> bit of the variable X. (X = X[0]    X[1]    X[2]    .....).
Y <sub>i</sub>	The <i>i</i> <sup>th</sup> block of the variable Y. (Y = Y <sub>0</sub>    Y <sub>1</sub>    Y <sub>2</sub>    ....).
ceiling(x)	The smallest integer greater than or equal to the real number <b>x</b> .
& <sub>n</sub>	The bitwise AND operation in an n-bit register.
<< <sub>n</sub> t	t-bit left shift in an n-bit register.
>> <sub>n</sub> t	t-bit right shift in an n-bit register.

### 3.3 Abbreviations

For the purposes of the present document, the abbreviations given in 3GPP TR 21.905 [1] and the following apply. An abbreviation defined in the present document takes precedence over the definition of the same abbreviation, if any, in 3GPP TR 21.905 [1].

CBC-MAC	Cipher Block Chaining Message Authentication Code
MAC	Message Authentication Code

## 4 Introductory information

### 4.1 Introduction

The confidentiality algorithm GEA5 is a stream cipher that is used to encrypt/decrypt blocks of data under a confidentiality key KC128. The block of data may be between 1 and 65536 octets long. The algorithm uses SNOW 3G [2] as a keystream generator.

The integrity algorithm GIA5 computes a 32-bit MAC (Message Authentication Code) of a given input message using an integrity key KI128. The approach adopted uses SNOW 3G.

### 4.2 Notation

#### 4.2.1 Radix

The prefix "0x" indicates hexadecimal numbers.

#### 4.2.2 Conventions

The assignment operator "=", as used in several programming languages.

$$\langle \text{variable} \rangle = \langle \text{expression} \rangle$$

means that  $\langle \text{variable} \rangle$  assumes the value that  $\langle \text{expression} \rangle$  had before the assignment took place. For instance,

$$x = x + y + 3$$

means

(new value of  $x$ ) becomes (old value of  $x$ ) + (old value of  $y$ ) + 3.

#### 4.2.3 Bit/byte ordering

All data variables in this specification are presented with the most significant bit (or byte) on the left hand side and the least significant bit (or byte) on the right hand side. Where a variable is broken down into a number of sub-strings, the left most (most significant) sub-string is numbered 0, the next most significant is numbered 1 and so on through to the least significant.

For example an  $n$ -bit MESSAGE is subdivided into 64-bit substrings  $MB_0, MB_1 \dots MB_i$  so if the message is:

0x0123456789ABCDEFEDCBA987654321086545381AB594FC28786404C50A37...

then:

$MB_0 = 0x0123456789ABCDEF$   
 $MB_1 = 0xFEDCBA9876543210$   
 $MB_2 = 0x86545381AB594FC2$   
 $MB_3 = 0x8786404C50A37\dots$

In binary this is:

0000000100100011010001010110011110001001101010111100110111011111111110...

with  $MB_0 = 00000001001000110100010101100111100010011010101111001101110111$   
 $MB_1 = 111111011011100101110101001100001110110010101000011001000010000$   
 $MB_2 = 1000011001010100010100111000000110101011010110010100111111000010$   
 $MB_3 = 1000011110000110010000000100110001010000101000110111\dots$

### 4.3 List of variables

CONSTANT-F a 32-bit parameter which is constant for any given FRAMETYPE input.



DIRECTION	the 1-bit input to both the GEA5 and GIA5 functions indicating the direction of transmission (uplink or downlink).
FRAMETYPE	an 8-bit input to the GEA5 and GIA5 functions indicating the type of frame to be protected.
INPUT	the 32-bit time variant input to the GEA5 function
INPUT-I	the 32-bit time variant input to the GIA5 function
KC128	the 128-bit confidentiality key.
KI128	the 128-bit integrity key.
KS[i]	the <i>i</i> th bit of keystream produced by the keystream generator.
L	the number of 32-bit words of SNOW 3G keystream that are generated by GEA5 (equal to $\text{ceiling}(M/4)$ ).
LENGTH	a 64 bit parameter defined within GIA5 which specifies the number of bits of message to be MAC'd (equal to 8 times M).
M	the input to the GEA5 function which specifies the number of octets of output required (1-65536); also the input to the GIA5 function which specifies the number of octets of message to be MAC'd (1-65536).
MAC	the 32-bit message authentication code (MAC) produced by the integrity function GIA5.
MESSAGE	the input bitstream of LENGTH bits that is to be processed by the GIA5 function.
OUTPUT	the output octets from the GEA5 function.
$S_1, S_2, \dots$	a sequence of 64-bit words derived from MESSAGE and LENGTH which is used within GIA5 to construct the MAC
$z_1, z_2, \dots$	the 32-bit words forming the keystream sequence of SNOW 3G. The word produced first is $z_1$ , the next word $z_2$ and so on.

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## 5 Confidentiality algorithm GEA5

### 5.1 Introduction

The confidentiality algorithm GEA5 is a stream cipher that encrypts/decrypts blocks of data between 1 and 65536 octets in length.

### 5.2 Inputs and outputs

The inputs to the algorithm are given in Table 5.2.1, the output in Table 5.2.2:

Table 5.2.1: GEA5 inputs

Parameter	Size (bits)	Comment
INPUT	32	Frame dependent input INPUT[0]...INPUT[31]
DIRECTION	1	Direction of transmission DIRECTION[0]
FRAMETYPE	8	Input value signifying the type of frame to be protected
KC128	128	Confidentiality key KC128[0]...KC128[127]
M		The number of octets of output required in the range 1 to 65536 inclusive

Table 5.2.2: GEA5 output

Parameter	Size (bits)	Comment
OUTPUT	8M	Keystream octets OUTPUT{0}...OUTPUT{M-1}

## 5.3 Components and architecture

This clause only available under licence.

See <http://www.etsi.org/about/what-we-do/security-algorithms-and-codes/cellular-algorithm-licences>.

## 5.4 Initialisation

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## 5.5 Keystream generation

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## 5.6 Output octets

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# 6 Integrity algorithm GIA5

## 6.1 Introduction

The integrity algorithm GIA5 computes a Message Authentication Code (MAC) on an input message under an integrity key KI128. The message may be between 1 and 65536 octets long.

For ease of implementation the algorithm is based on the same stream cipher (SNOW 3G) [2] as is used by the confidentiality algorithm GEA5.

## 6.2 Inputs and outputs

The inputs to the algorithm are given in table 6.2.1, the output in table 6.2.2:

Table 6.2.1: GIA5 inputs

Parameter	Size (bits)	Comment
INPUT-I	32	Frame dependent input INPUT-I[0]...INPUT-I[31]
M		The length of MESSAGE in octets (1-65536)
MESSAGE	8M	Input octet stream MESSAGE{0}...MESSAGE{M-1}
DIRECTION	1	Direction of transmission DIRECTION[0]
FRAMETYPE	8	Input value signifying the type of frame to be protected
KI128	128	Integrity key KI128[0]...KI128[127]

Table 6.2.2: GIA5 output

Parameter	Size (bits)	Comment
MAC	32	Message authentication code MAC[0]...MAC[31]

## 6.3 Components and architecture

### 6.3.1 SNOW 3G

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### 6.3.2 MULx

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### 6.3.3 MULxPOW

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### 6.3.4 MUL

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## 6.4 Initialization

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## 6.5 Calculation

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## Annex A (informative): Mathematical background of some operations of the GIA5 Algorithm

### A.1 The function EVAL\_S

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### A.2 The function MUL(V, P, c)

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## Annex B (informative): Implementation options for some operations of the GIA5 algorithm

### B.1 Overview

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### B.2. Procedure Pre\_Mul\_P

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### B.3 Function Mul\_P

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## Annex C (informative): Figures of the GEA5 and GIA5 algorithms

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## Annex D (informative): Simulation program listing

### D.1 GEA5

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### D.2 GIA5

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## Annex E (informative): Change history

Change history							
Date	Meeting	TDoc	CR	Rev	Cat	Subject/Comment	New version
2016-04	SA3#83		-	-	-	First Draft	0.1.0
2016-04	SA3#83		-	-	-	Removed algorithm details until permission to publish is received from French Government.	0.0.2
2016-04	SA3#83		-	-	-	Updated version sent to French Government for permission to publish	0.2.0
2016-05	SA3#83		-	-	-	Updated titles after comments in SA3 #83	0.2.1
2016-05	SA3#83		-	-	-	Removed algorithm details until permission to publish is received from French Government.	0.2.2
2016-11	SA3#85		-	-	-	Full Specification with Example Code	0.3.0
2016-06	SA#72	SP-160380				EditHelp editorial fix and presented for information	1.0.0
2016-11	SA3#85					Updated version only	1.1.0
2016-11	SA3#85					Updated the editors note to reflect the need for a licence to see the content	1.1.1
2016-11	SA#74	SP-160792				MCC clean up, redacted version for TSG SA approval	2.0.0
2016-12	SA#74					Approved by TSG SA	13.0.0
2017-03	SA#75	-	-	-		Promotion to Release 14 without technical change	<b>14.0.0</b>
2018-06	-	-	-	-	-	Update to Rel-15 version (MCC)	<b>15.0.0</b>



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# History

<b>Document history</b>		
V15.0.0	July 2018	Publication